

International Institute for  
Technology and Management



## Tutoring Sheet # 18

Unit 05a : Mathematics 1

1. a.) Use the Lagrange multiplier method to find the values of  $x$  and  $y$  That maximize the function  $f(x,y) = xy^{2/3}$  subject to the constraint  $x + 2y = 100$  .  
b.) Use the Lagrange multiplier method to find the values of  $x$  and  $y$  That maximize the function  $f(x,y) = 3\sqrt{x} + 4\sqrt{y}$  subject to the constraint  $x + y = 100$  .  
c.) Optimize  $f(x,y) = 120x - 4x^2 + 2xy - 3y^2 + 96y - 222$  subject to the constraint  $x + 3y = 69$   
d.) Use the Lagrange multiplier method to find the values of  $x$  and  $y$  That maximize the function  $f(x,y) = \sqrt{x} y^2$  subject to the constraint  $x + y = 100$  .
  
2. A firm has weekly production function  $q(k,l) = k^{1/4} l^{1/2}$  and the unit weekly costs for capital and labour are  $v = 20$  and  $w = 10$  . the firm wishes to produce 200 units a week of its good. Find the minimum cost of doing so.
  
3. Study Guide page 95 : **Question 5** .
  
4. Study Guide page 95 : **Question 6** .
  
5. Study Guide page 95 : **Question 7** .
  
6. Study Guide page 95 : **Question 8** .