

Unit 05a: Mathematics 1 – (MathA)

1. Determine the derivatives of the following functions :

a. $y = (3\ln x - x)(\ln x - 2)^2$

b. $y = (\sqrt{1+x^2})e^x$

c. $y = \frac{x^2 - 1}{x} + e^{\frac{-x^2}{2}}$

d. $y = \sqrt{\frac{1-x}{1+x}}$

e. $y = \frac{1 - \sin x}{1 + \sin x}$

f. $y = \ln(\sqrt{x + \sqrt{x}})$

(18 Marks)

2. Find all stationary points of the following functions and determine whether they are maxima, minima or inflection points:

(12 Marks)

a. $y = x^4 - \frac{5}{3}x^3 + \frac{1}{2}x^2$

b. $y = \frac{x^2 - x + 1}{x}$

c. $y = x^2 \ln x$

3. Find all stationary points of the following function and Specify their nature:

(8 Marks)

$$f(x) = \frac{1}{12}x - \sqrt[3]{x}$$

4. A firm has average variable cost

(6 Marks)

$$q + 5e^{2q^2 - 1} + \frac{\ln(2q^2 - 1)}{q}$$

and fixed costs of 8. Find the total cost function and the marginal cost function.

5. Find the values of the constant $a \neq 0$ for the which the function

$$f(x) = \ln x - \frac{2}{a}x^2$$

admits a maximum.

(6 Marks)

END of QUESTIONS