



# Differential Equations

## Tutoring Sheet #16

1. Solve the following Differential Equations:

a.  $y'' = xe^x$

b.  $2\sqrt{x} \frac{dy}{dx} = x^2 - 1$

c.  $(2x + 3y)dx + (y - x)dy = 0$

d.  $y \frac{dy}{dx} = \sqrt{y^2 + 1}$

e.  $x^3 dx + (y+1)^2 dy = 0$

f.  $\frac{dy}{dx} = \frac{y(x+2y)}{x(2x+y)}$

2. Solve the following differential equations:

a.  $\frac{dy}{dx} + 2y = 8x^2 - 2$

b.  $x \frac{dy}{dx} + 3y = 2x + 5$

c.  $x^2 \frac{dy}{dx} + xy + y = 0$

d.  $\frac{dy}{dx} = (x+y)^2$

e.  $\frac{d^2y}{dx^2} - \frac{dy}{dx} - 6y = 3x^2 + x + 2$  If  $y = 1$  and  $\frac{dy}{dx} = 1$  when  $x = 0$

f.  $\frac{d^2y}{dx^2} - \frac{dy}{dx} - 2y = e^{2x}$

g.  $\frac{d^2y}{dx^2} - 2 \frac{dy}{dx} - y = \sin x$

h.  $\frac{d^2y}{dx^2} + y = \sin x + \cos x$

i.  $\frac{d^2y}{dx^2} + \frac{dy}{dx} - 6y = e^{2x} \cos x$

j.  $\frac{d^2y}{dx^2} - 4 \frac{dy}{dx} + 4y = 8(x^2 + \sin 2x)$

k.  $\frac{d^2y}{dx^2} + 4y = \cos 2x + \cos 4x$