



Integration II

Handout #16

$f(x)$	$\int f(x) dx$
K , K is a Constant Examples: $\int 5 dx$ $\int dx$	$Kx + C$ $5x + C$ $x + C$
x^n , $n \neq -1$ Examples: $\int x^7 dx$ $\int (2x^3 - 5x - 1)dx$	$\frac{x^{n+1}}{n+1} + C$ $\frac{x^{7+1}}{7+1} + C = \frac{x^8}{8} + C$ $2\frac{x^4}{4} - 5\frac{x^2}{2} - x + C = \frac{x^4}{2} - \frac{5x^2}{2} - x + C$
e^x e^{ax} Examples: $\int e^{3x} dx$ $\int e^x (e^x - 2)dx$	$e^x + C$ $\frac{1}{a} e^{ax} + C$ $\frac{1}{3} e^{3x} + C$ $\int (e^{2x} - 2e^x)dx = \frac{1}{2} e^{2x} - 2e^x + C$
$\int \frac{dx}{x}$ $\int \frac{dx}{ax+b}$ Example: $\int (t+1 - \frac{4}{t+2})dt$	$\ln x + C$ $\frac{1}{a} \ln(ax+b)$ $\frac{t^2}{2} + t - 4 \ln(t+2) + C$



$f(x)$	$\int f(x) dx$
Sinx	$-\cos x + C$
Sin ax	$\frac{-1}{a} \cos ax + C$
Example: $\int (x + \sin 2x) dx$	$\frac{x^2}{2} - \frac{1}{2} \cos 2x + C$
Cosx	$\sin x + C$
Cos ax	$\frac{1}{a} \sin ax + C$
Example: $\int (2 + \cos 3x) dx$	$2 + \frac{1}{3} \sin 3x + C$
Example: Calculate: $\int_1^2 \frac{\sin(\ln x)}{x} dx$	<p>Let $u = \ln x \Rightarrow du = \frac{dx}{x} \Rightarrow \int_1^2 \frac{\sin(\ln x)}{x} dx = \int_1^2 \sin u du = -\cos u$</p> $= [-\cos(\ln x)]_1^2 = -\cos(\ln 2) - [-\cos(\ln 1)] = -\cos(\ln 2) + \cos 0$ $= -\cos(\ln 2) + 1 = 1 - \cos(\ln 2) \quad \{ \text{since } \ln 1 = 0 \}$
Example: $\int t e^{t^2} dt$	<p>Let $u = t^2 \Rightarrow du = 2t dt \Rightarrow t dt = \frac{du}{2}$</p> $\int t e^{t^2} dt = \int e^u \frac{du}{2} = \frac{1}{2} \int e^u du = \frac{1}{2} e^u + C = \frac{1}{2} e^{t^2} + C$